A C++ Programme for Global Optimization

Serguei Zertchaninov* and Kaj Madsen

Abstract} A stochastic Branch-and-Bound Method for global optimization over a compact right parallelepiped, parallel to the coordinate axes, has been developed, described and tested in ([1],[2]). This report describes the C++ implementation of the method. Section 2 is a short description of the new method, Section 3 provides some implementation details, and Section 4 is a user’s guide to the programme. The source code of the implementation is available on request to the authors.

1 Introduction

It is well known that many problems in industry and economy can be formulated as mathematical programming problems, i.e. as the minimization of a function $f : D \rightarrow \mathbb{R}$ where $D \subseteq \mathbb{R}^n$. Dimensionality $n$ of such functions usually is quite large. Besides that, very often the function $f$ has several local minima in the region of interest. However, only the smallest one is interesting:

$$f^* \equiv \inf \{ f(x) \mid x \in D \}$$

(1)

$f^*$ is called the global minimum and the set of points where it is attained is called the set of global minimizers.

The problem of creating an algorithm (a computer program) which is guaranteed to find this set has not been solved, and it probably will never be. Interval analytic methods only solve the problem for a limited class of problems. Most other methods either give no guarantee for convergence or convergence is so slow that for larger dimensions it is unrealistic. Some techniques require ‘help’ of a skilled engineer who uses his insight into the technical problem which is modeled. This can lead to solutions which could not have been found by fully automatic optimization methods.

The purpose of this project is to develop an automatic optimization method. Having the exponential complexity of the global optimization problem in mind we don’t intend to guarantee the solution is found, but rather to try to get the best possible out of a given amount of computational resources. The user should specify how much computer time and storage he will spend rather than specifying some epsilon accuracy as required by many traditional approaches.

Since the classical deterministic method based on interval arithmetic has been very successful we base our new technique on the same general branch-and-bound principle,

*on leave from Informatics Department, Nizhnij Novgorod State University
but without the requirement that interval arithmetic must be applicable. Thus the new method is a strategy for managing local methods (like quasi-Newton methods) in a branch-and-bound search for global minimizers.

This report consists of several sections. In Section 2 we give a general description of the new method. The details of implementation are given in Section 3. Recommendations in Section 4 tell how to use this program. In Section ?? we provide some computational results.

2 Description of the method

We start the description with introducing some terms which will be used in further material. Let function be a given real function of \( n \) variables. Let box be an \( n \)-dimensional real interval. We assume that function is defined in some box, i.e. has interval constraints. Let \( C \), or candidate set, be a set of boxes to test. Let \( G \), or garbage set, be a set of boxes temporarily eliminated from the search. We define the value \( f_{\text{bound}} \) which is the smallest function value found during the search. Temporary value \( B \) is used to store a single box. Thus the structure of the new algorithm is the following:

\[
\text{initialize} \rightarrow C, f_{\text{bound}}, G
\]

\[
\text{while} \; \text{true do}
\]

\[
\text{while} \; C \neq \emptyset \; \text{do}
\]

\[
\text{remove-best}(C) \rightarrow B
\]

\[
\text{reduce-or-subdivide}(B) \rightarrow \text{result}, f_{\text{bound}}, \text{garbage}
\]

\[
C = C \cup \{\text{result}\}
\]

\[
G = G \cup \{\text{garbage}\}
\]

\[
\text{end}
\]

\[
\text{while} \; G \neq \emptyset \; \text{do}
\]

\[
\text{remove}(G) \rightarrow B
\]

\[
\text{split}(B) \rightarrow \text{result}
\]

\[
C = C \cup \{\text{result}\}
\]

\[
\text{end}
\]

\[
\text{end}
\]

The \texttt{initialize} procedure is called when the method is started the first time, and every time when the method runs out of memory. It clears both \( C \) and \( G \) sets, then adds the initial box together with the best points of minimum, found in the previous iterations, to \( C \) set. Obviously, there are no such points when the method starts the first time. In this case \( f_{\text{bound}} \) value is also initialized.

The purpose of the outer \texttt{while}-loop is to let the program run for as long as the user wants. When time is out the program stops providing the best estimate of the global optimizers that has been found. The longer time used, the better result should be expected. For small dimensions, however, the whole set of global minimizers should normally be found in a rather modest amount of computer time.
Inside the first inner while-loop the actual search procedures are being performed. remove-best procedure removes the best box from the candidate set and stores it in $B$. reduce-or-subdivide performs two consequential actions. At first, using different testing procedures such as monotonicity test and quasi-newton search, it determines whether box should be eliminated from the candidate set or not. At second, using the conclusion obtained on the first stage, it places the box to the garbage or splits it into two parts for further exploration. Let us take a closer look at how reduce-or-subdivide works.

**Sampling:** To prepare the box for testing method samples a certain amount of points inside the box. It uses two strategies for placing these points. The first way is to use some regular distribution. Method places one point in the center of the box, and for each coordinate it places two points, shifted from the center along the axes to the left and to the right on the same value in percent to appropriate side length. Such point we will call regular. The second way is to use random points, uniformly distributed in the box. These we will call random points. For each point the function value is calculated.

**Monotonicity test:** This test uses a certain number of sampled points to check the monotonicity. If it proves function in the box is monotonous the box is placed to garbage. But here we should mention that the monotonicity test is skipped in our implementation because this has proved most efficient in our tests. The possible reason for inefficiency of monotonicity test is the following: after the first loop each full rank box in $C$ contains at least one local minimum (because of subdivide below), and thus $f$ is not likely to be monotone in any of these boxes.

**Newton-test:** From the given number of sampled points method starts local search sequences to find stationary points located inside the box. The local technique used in our tests is a version of the dog-leg method, [3], which allows for an easy control of the step lengths. Gradient in every point generated by local method is used to update maximal gradient value. We distinguish three pictures of convergency: If all iteration sequences go out of $B$ then $B$ is placed to garbage. If all starting points lead to iteration sequences converging to the same point $x \in B$ then $\{x\}$ is placed to result and $B$ is added to garbage. If none of the two situations take place then we have found several local minima in $B$. Then method estimates the lower bound of the function in the box $LB(B)$. It takes all points, generated by sampling procedure, and maximal gradient value to calculate $LB(B)$ as follows:

$$LB(B) = \min_{i \neq j} \frac{f(x_i) + f(x_j) - \text{maxgrad}\|x_i - x_j\|^2}{2}$$

(3)

$LB(B)$ is corrected if it is greater than the lowest minimum found in the box. Finally, if $LB(B) > f_{\text{bound}}$ then box is added to garbage. Else subdivide procedure should be performed.

**Subdivide:** In this case $B$ contains several known local minima, and the splitting into two is done so each new box contains (known) local minima. There are several ways of achieving such a subdivision. We will give more detailed description in the next section.

The first while-loop runs until the candidate set is empty. It also can be interrupted if method runs out of memory. In this case the initialization procedure is called. If method runs out of time limit, it stops. If there was no interruption method proceeds with the second inner while-loop.

3
In the second inner while-loop the garbage set is emptied. \textbf{remove} procedure takes one box from the garbage set and stores it in $B$. Then this box is split into two parts by \textbf{split} procedure. It uses different splitting approaches depending on the amount of stationary points found in the box.

If there are no such points, the box is subdivided in two equal parts by plane, crossing the center of the box and perpendicular to the side with the maximal length. If there is only one stationary point in the box then method finds the coordinate for which the distance from the point to the border is maximal. The splitting plane is chosen to be perpendicular to this coordinate axis, and it is shifted from the point to a certain value in the direction where distance to the border is maximal. In case of multiple stationary points \textbf{subdivide} procedure from above is used.

The second while-loop runs until the garbage set is empty. It also can be interrupted if method runs out of memory. In this case the initialization procedure is called. If method runs out of time limit, it stops. If there was no interruption method proceeds with the first inner while-loop, and so on.

## 3 Implementation

To implement this method C++ programming language was used. We organized all data and procedures as C++ classes, each representing a quite independent part of the search process. There are two groups of classes: main and supplementary. The main group classes are the following: \textit{TProblem} - a class containing data and routines for calculating function and first derivative values, and for managing the results output; \textit{TMethod} - a class providing procedures for box testing; \textit{Process} - a class which contains all data structures and procedures necessary for managing the search, including \textit{TProblem} and \textit{TMethod} objects. The supplementary group contains storage classes: \textit{TTrial} - a class to represent a single point; \textit{TBox} - a class representing a box with points inside; \textit{TBoxList} - a class designed to store ordered list of boxes. There are also two classes to implement vectors and matrices - \textit{TVector} and \textit{TMatrix}, which will not be described here.

Let us consider a supplementary group of classes. We will not describe all data members and functions but only the most important ones. First class is \textit{TTrial} - quite trivial one as all data are public:

```cpp
class TTrial
{
public:
    TVector XVal; // vector of real values, or a point
    double FVal; // corresponding function value
    PTTrial Next; // pointer to next TTrial in a list

    TTrial(int); // constructor by size of XVal vector
    TTrial(RTTrial); // copy constructor
    RTTrial operator=(RTTrial); // assignment operator
    int GetXDim(); // returns dimension of XVal vector
    long int SizeOfTrial(); // returns memory required for storing TTrial
```

Let us consider a supplementary group of classes. We will not describe all data members and functions but only the most important ones. First class is \textit{TTrial} - quite trivial one as all data are public:
Function SizeOfTrial() returns amount of memory in \textit{sizeof(char)} units required to store one object of TTrial class. It is used in procedures responsible for memory checks. All other functions and data members of TTrial are quite obvious. Class TBox is the second basic storage class, and it looks like following:

```cpp
class TBox
{
    public:
        TVector Right; - vector of right boundaries
        TVector Left; - vector of left boundaries
        PTTrial Pts; - list of points located in the box
        double CMin; - current minimum in the box
        PTBox Next; - pointer to next TBox in a list
        TBox(int); - constructor by dimensionality
        TBox(R TBox); - copy constructor
        TBox(); - destructor
        int Insert(PTTrial); - inserts trial to the box
        int AddCopy(PTTrial); - inserts copy of trial to the box
        PTTrial GetBest(); - returns pointer to the best trial
        PTTrial RemoveBest(); - removes the best trial from the list
        void Clear(); - clears trials list
        int GetAmount(); - returns number of trials in the list
        int InBox(PTTrial); - returns TRUE if trial is inside the box
        int GetXDim(); - returns dimension of the box
        int GetType(); - returns type of the box
        int NearToMin(PTTrial,double); - checks distance to the points
        void Truncate(double); - discards trials with too high function values
        double GetLongSide(); - returns length of the longest side
        double GetShortSide(); - returns length of the shortest side
        double GetMaxSlope(); - estimates maximal slope of function
        double GetLBound(double); - estimates lower bound of function
        long int SizeOfBox(); - returns memory required for storing TBox
        static long int GetMemUsed(); - returns memory used for trials
};
```

There is a group of functions performing operations with the list of points. It is possible to insert a point or a copy of the point into the list, obtain pointer to the best point in the list, remove it from the list, get total number of points in the list, and clear the list of points.

Function InBox(PTTrial \texttt{tr}) checks whether given point \texttt{tr} located inside the box or not. Do not be confused - it does not check whether the point is in the list. Function
GetType() returns one of the predefined box type constants. There are three of them: for empty box, for box containing only one point in its list, and for box with several points inside. Function NearToMin(PTRial, double dist) checks whether given point tr located close to one of the points in the list or not. Parameter dist gives the distance limit. Function Truncate(double band) removes points with function values greater than CMin + band. Function GetMaxSlope() estimates maximal slope of the function in the box using points from the list. The maximal slope is calculated as follows:

\[
MS = \max_{i \neq j} \frac{\| f(x_i) - f(x_j) \|}{\| x_i - x_j \|}
\] (4)

Function GetLBound(double slope) estimates lower bound of the function in the box using point from the list. It uses Formula 3 for calculations, where maxgrad is given by slope parameter. Function SizeOfBox() returns amount of memory in sizeof(char) units required to store one object of TBox class. Function GetMemUsed() returns amount of memory used by all TTrial objects stored in all TBox objects available. Two last functions are used in procedures responsible for memory checks.

Class TBoxList serves for storing ordered list of boxes. Boxes in the list are ordered by their CMin values in increasing order. So the best box is always at the beginning of the list. There are the same basic operations for including and removing a box as in class TBox for points. Definition of TBoxList looks like following:

```c++
class TBoxList
{
    PTBox List; - list of boxes
    static long int BCount; - memory counter for stored boxes
    public:
        TBoxList(); - default constructor
        TBoxList(); - destructor
        int Insert(PTBox); - inserts box in the list
        int AddCopy(PTBox); - inserts copy of the box in the list
        PTBox GetBest(); - returns pointer to the best box
        PTBox RemoveBest(); - removes the best box from the list
        void Clear(); - clears list of boxes
        int GetAmount(); - returns number of boxes in the list
        int IsEmpty(); - returns TRUE if list is empty
        static long int GetMemUsed(); - returns memory used for boxes
};
```

Function IsEmpty() returns boolean true in case when list of boxes is empty. Function GetMemUsed() returns amount of memory used by all TBox objects stored in all TBoxList objects available.

Let us consider now the main group of classes. There are three classes in this group, and we start with class TProblem. As it was mentioned above TProblem contains data
and routines for calculating function and first derivative values, and for managing the results output. It is defined like follows:

class TProblem
{
    double FBand; - band for minimal function values
    double CMin; - current estimation of minimum
    long int FCount; - number of function calculations
    long int DFCount; - number of derivative calculations

    FILE* ResFile; - results file pointer
    char* ResName; - results file name

protected:
    int OpenResults(); - opens results file
    int CloseResults(); - closes results file
    int WriteResults(); - writes to results file

    virtual void PureCalcF(PTTrial)=0; - calculates F(X)
    virtual void PureCalcDF(PTTrial,PTVector)=0; - calculates F'(X)
    virtual void PureCalcF_DF(PTTrial,PTVector)=0; - calculates F(X) and F'(X)

public:
    TBox Bounds; - area of definition and points of minimum

    TProblem(PTBox,double,char*); - constructor by bounds,fband,filename
    virtual TProblem(); - destructor

    int CalcF(PTTrial); - calculates F(X)
    int CalcDF(PTTrial,PTVector); - calculates F'(X)
    int CalcF_DF(PTTrial,PTVector); - calculates F(X) and F'(X)
    int InBounds(PTTrial tr); - point is in bounds
    int AddToResults(PTTrial); - adds trial to results list
    int GetXDim(); - returns dimension of the function
    double GetCMin(); - returns current minimum
    double GetFBand(); - returns function band for minima
    long int GetFCount(); - returns number of F(X) calculations
    long int GetDFCount(); - returns number of F'(X) calculations
}

Within the definition of the class one can see three pure virtual functions. They were introduced to allow for different implementation of function and first derivatives. User needs to derive classes based on TProblem class where those virtual functions will be defined. Currently we have two such classes ready to use: class TProblemFF for calculating function given as a C procedure, and class TProblemDD for calculating first derivatives
using simple divided differences. They are incomplete classes because only function or derivative calculations are implemented in each one. But to make a useful class we need to combine these two calculations. So we created class TProblemFFDD derived from both of them. This class is actually used in our program.

Let us return to the class TProblem. Functions PureCalcF(), PureCalcDF(), PureCalcF_DF() are virtual functions calculating function and first derivative values without any border checks and updating any internal variables. These checks and updates are made by corresponding functions without Pure- prefix, from which those virtual functions are called. Namely, they check given point for being located within given problem boundaries, update current minimum value CMin, and increment corresponding counters - FCount and DFCount.

Another group of procedures is responsible for creating the results output. ResFile and ResName are results file pointer and results file name respectively. File is opened by procedure OpenResults(), information is written by WriteResults(), and it is closed by CloseResults().

The result this method provide is a set of stationary points with best function values found during the search. This set of points is stored in the internal list of Bounds box. To prevent TProblem from storing points with too high function values FBand data member is used. Thus only points with function values less or equal to CMin + FBand will be stored. It is recommended to set FBand to some small value, equal or close enough to the method accuracy, in case if user wants to get only possible global minimizers as a result. Function AddToResults() adds a point to the results list.

The second main class to consider is TMethod - a class providing procedures for box testing. Its definition is following:

class TMethod
{
    double Accuracy; - search accuracy
    double AttractR; - radius of attraction
    int RandAmnt; - number of random points
    int NewtAmnt; - number of points to start newton search

    int DogLegStep(PTProblem,PTBox,RTTrial,RTVector,
                            RTMatrix,RTMatrix,double&); - performs dog-leg iteration

protected:
    void FillRegular(PTProblem,PTBox); - samples regular points
    void FillRandom(PTProblem,PTBox); - samples random points
    virtual void FillBox(PTProblem,PTBox); - samples points in the box
    virtual double DoSearch(PTProblem,PTBox,PTBox); - searches for minima

public:
    TMethod(double,double,int,int); - constructor by accuracy,attr.R,random,start
    int CheckBox(PTProblem,PTBox); - checks function behavior in the box
    double GetAccuracy(); - returns accuracy
double GetAttractR(); - returns radius of attraction
int GetRandAmnt(); - returns number of random points
int GetNewtAmnt(); - returns number of starting points
}

There is only one single procedure which is called from TPProcess object to check a box - it is CheckBox(). It corresponds to reduce-or-subdivide procedure from Section 2. A box to test is passed together with the problem to this function.

Sampling is made by function FillBox() which, in its turn, calls functions FillRegular() and FillRandom() to sample regular and random points respectively. The number of random points to sample is given by RandAmnt data member. We use standard library random generator rand() with uniform distribution. FillBox is defined virtual to allow user to implement some different sampling strategy.

Local search is done by function DoSearch() which starts search sequences from the number of sampled points given by NewtAmnt data member. It takes only the best NewtAmnt points to start. The first box in the parameters list is an original box, and all stationary points, which will be found during the local search, are added to this box. The second box is one with a set of sampled points. DoSearch() returns real value - maximal gradient component found, later used to estimate the lower bound of the function in the box. Data member Accuracy gives an accuracy of local search. AttractR data member gives the radius of a hypersphere, surrounding each point of local minimum. It is needed to prevent local search from converging to the same point several times. Its value depends significantly on the technique for calculating derivatives, and on the local search method itself. Ideally it should be equal to accuracy, but in our tests we used a greater value. In this implementation we use divided differences for calculating derivatives and dog-leg local search procedure.

The result of applying CheckBox() is one of the predefined constants describing what should be done with the box. There are two possible actions: eliminate box from the candidate set, or split it into two parts placing them back into candidate set. These actions are carried out by TPProcess object.

Class TPProcess contains all data structures and procedures necessary for managing the search, including TProblem and TMethod objects. It is defined like follows:

class TPProcess
{
    PTProblem Pr; - pointer to problem object
    PTMethod Met; - pointer to method object

    long int MaxBytes; - memory limit
    long int MaxTime; - time limit
    time_t StartTime; - start time

protected:
    int SplitBox(PTBox); - splits given box in two
public:
    TBoxList Unexplored; - candidate list
    TBoxList Eliminated; - garbage list

    TProcess(PTProblem,PTMethod,long int,long int);
    - constructor by problem,method,memory,time
    int PrepareLists(); - prepares lists of boxes for performing a cycle
    int DoIteration(); - performs one iteration of the method
    int DoProcess(); - performs whole search process
    int InMemory(); - returns memory status
    int InTime(); - returns time status
    long int GetMaxBytes(); - returns memory limit
    long int GetMaxTime(); - returns time limit
    long int GetMemory(); - returns amount of used memory
    long int GetTime(); - returns time from start
};

Pointers to TProblem and TMethod objects are passed by constructor parameters and stored afterwards in Pr and Met data members. Thus they should be created outside the TProcess object. It gives a good flexibility as different problem and method implementations can be used.

There are two objects of TBoxList class in the public area - Unexplored and Eliminated. They correspond to the candidate and garbage sets respectively. We have placed them both in a public area in order to allow user to get access to the information they contain.

The main procedure which performs the whole search process is DoProcess(). It quits when the time limit given by MaxTime data member is finished. Its internal structure is quite simple and looks like that:

```
int DoProcess()
{
    while (PrepareLists())
        while (DoIteration());
    return TRUE;
}
```

The outer while-loop here corresponds exactly to the outer loop in the description of the method from Section 2. It runs until the value returned by PrepareLists() function becomes false, which happens when the time limit is finished.

Function PrepareLists() contain both initialization procedure and second outer loop described in Section 2. It initialize the internal data when it is necessary namely in case if process starts the first time, or if it is restarted due to running out of memory. Then, in a while-loop, it fetches boxes from the Eliminated list to split them and put into the Unexplored list.

The inner while-loop here corresponds exactly to the first inner loop in the description of the method from Section 2. All actions inside the loop are carried out by DoIteration() procedure which is shown below:
int DoIteration()
{
    if (!InTime() || !InMemory()) return FALSE;
    PTBox temp=Unexplored.RemoveBest();
    if (temp==NULL) return FALSE;
    if (Met->CheckBox(Pr,temp)==ACTION_SPLIT) SplitBox(temp);
    else Eliminated.Insert(temp);
    return TRUE;
}

The first if operator checks for time and memory conditions. In the second line the best box from the candidate set is removed and stored in temporary variable. The second if operator checks whether candidate set was empty or not, as a null pointer is returned in a case of empty set. The last if operator calls method function to check the box, and a resulting value is compared with one of the predefined action constants. If returned value is equal to ACTION_SPLIT then SplitBox() procedure is applied to the box. Else, namely when returned value is equal to ACTION_ELIMINATE, the box is placed into the garbage set.

Function SplitBox() is called every time a box has to be split, either from inside of PrepareLists() function or DoIteration() function. It always splits a box in two parts and places those into the candidate set. The initial box is deleted but all the points it contained are distributed to new pair of boxes. The procedure recognizes three types of boxes and applies different split subroutines for each type. Empty box is subdivided in two equal parts by plane, crossing the center of the box and perpendicular to the side with the maximal length. If there is only one stationary point in the box then coordinate, for which the distance from the point to the border is maximal, is selected. The splitting plane is chosen to be perpendicular to this coordinate axis, and it is shifted from the point to a certain value in the direction where distance to the border is maximal.

In case of multiple stationary points several split strategies can be applied. We have experimented with three of them. At first, we tried to use some kind of statistics. The central point for all $P$ stationary points in the box was computed by a simple formula:

$$Center = \frac{1}{P} \sum_{i=1}^{P} X_i$$  \hfill (5)

Then a vector of relative deviations, or dispersions, was calculated for this central point:

$$Dispersion = \frac{1}{P} \sum_{i=1}^{P} (Center - X_i)^2$$  \hfill (6)

Finally, the coordinate

$$k = \arg \max_i Dispersion[i]$$

was chosen. The box was subdivided in two by plane, crossing the Center point and perpendicular to $k$-th coordinate axis. This strategy gave rather good results but it is also a little bit expensive from computational point of view. Thus another approach was
introduced. Instead of using all $P$ stationary points contained in a box for calculations described above we suggested to consider only two of them with best function values. This strategy is used by default in current implementation. At last, we tried an additional rule which prevented splitting plane from intersecting with any stationary point in the box, but it required even more computations than in the first case, and gave no significant improvement as probability of such an intersection is very small.

4 How to use this program

In this section we illustrate how to write the complete program using our code. The short example program is given below for the purpose:

```c
001 #include "process.h"
002 extern const int DIM;
003 extern double F(TVector);
004 int main()
005 {
006   TBox Bounds(DIM);
007   Bounds.Right(0)=10.0;
008   Bounds.Left(0)=-10.0;
009   ...
010   long int Memory=640000;
011   long int Time=300;
012   char FileName[]="results.out";
013   double Accuracy=0.001;
014   double ARadius=0.1;
015   double FBand=0.001;
016   double DFStep=0.0001;
017   int Random=0;
018   int Start=DIM;
019   TProblemFFDD Prob(F,&Bounds,FBand,DFStep,FileName);
020   TMethod Met(Accuracy,ARadius,Random,Start);
021   TProcess Proc(&Prob,&Met,Memory,Time);
022   Proc.DoProcess();
023   return TRUE;
024 }
```

In line 001 the header file `process.h` which contains all necessary declarations is included. Lines 002 and 003 contain declarations of external objects: integer constant `DIM` - dimensionality of the problem, and real function $F$ of `TVector` - function to be minimized. Of course, it is not necessary to use dimensionality constant, and here it is given just for illustrative purpose. Function can also be defined in the same file.

From line 004 C function `main` begins. In line 006 object `Bounds` of class `TBox` is created. It will contain function constraints, which are assigned further in lines 007 and 008. Here we only show initialisation of the first component, and ellipsis in line 009
represents the part of code where the rest of components are initialized. Naturally, user is free to choose how to perform initialisation of bounds: in linear part of code, in loop or in some other way.

In the part of code from line 010 to line 018 all the parameters needed to start search are defined. In this example we assign some values which are not essential and probably they will be changed in a real application. Two integer values - Memory and Time represent memory and time limits. Character string FileName contains a name of file where results should be written. Two real values - Accuracy and ARadius define the local search accuracy and radius of attraction respectively. Real values FBand and DStep give band for minimal function values and step for calculating first derivatives. And, finally, integer values Random and Start represent number of random points and number of points to start local search. We should note that it is not necessary to define special variables for all these parameters but they can be written directly in the parameter lists of constructors.

In line 019 object Prob of class TProblemFFDD is created. This class is derived from class TProblem and supplies procedures for calculating function, given as a C function (see line 003), and for calculating first derivatives by using divided differences. Parameters of constructor are the following: function to minimize, pointer to bounds object, band for minimal function values, step for calculating first derivatives and results file name.

Object Met of type TMethod is created in line 020. Parameters of its constructor are the following: local search accuracy, radius of attraction, number of random points and number of points to start local search.

The last object needed to start running is created in line 021 - object Proc of class TProcess. The following parameters are passed to its constructor: pointer to problem object, pointer to method object, memory limit and time limit.

The whole search process is performed by call of a single function in line 022 - function DoProcess() of object Proc. It runs until the time limit is up. When the search is finished all the information is available through object Proc, namely, the lists of boxes can be read and modified, the solutions list and results file can be read and modified as well. After modifying some data process can be restarted. The results file will contain sequential blocks of data showing the progress in finding minimizers. Each block has the following format:

NUMBER OF F(X) AND F'(X) CALCULATIONS
number of function and first derivative calculations on the moment when the modification of the results list occured. Modified results list is printed after this header.

RESULTS LIST
results list in format:
  F(X) VALUE 1 : (X) VALUE 1
  F(X) VALUE 2 : (X) VALUE 2
  ...

Function main exits in line 023 and returns boolean TRUE as a result. As one can see, only about 30 lines of code are needed to write the complete program. We dare to assume
that our program is quite easy to use and it allows for an easy control of the search data. For deeper understanding please refer to the program source code and header files. These sources are available on request to the authors.

References

